



PROGRAMMING AND OPTIMIZATION FOR INTEL[®] ARCHITECTURE

Hands-On Workshop (HOW) Series "Deep Dive"

Session 10

Colfax International — colfaxresearch.com

April 2017

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- ▶ **Module I. Programming**
 - 01. Intel Architecture and Modern Code – Apr 17
 - 02. Xeon Phi, Coprocessors, Omni-Path – Apr 18
- ▶ **Module II. Expressing Parallelism**
 - 03. Automatic vectorization – Apr 19
 - 04. Multi-threading with OpenMP – Apr 20
 - 05. Distributed Computing, MPI – Apr 21
- ▶ **Module III. Optimization**
 - 06. Optimization Overview: N-body – Apr 24
 - 07. Scalar tuning, Vectorization – Apr 25
 - 08. Common Multi-threading Problems – Apr 26
 - 09. Multi-threading, Memory Aspect – Apr 27
 - 10. Access to Caches and Memory – Apr 28

April 2017						
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■ — Webinar+remote access

Course page:

colfaxresearch.com/how-17-04

- ▶ Slides
- ▶ Code
- ▶ Video
- ▶ Chat

More workshops:

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GET YOUR QUESTIONS ANSWERED: CHAT



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GET YOUR QUESTIONS ANSWERED: FORUMS

	READ	WATCH	LEARN	FORUMS	CONNECT	JOIN
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Forum

Colfax Cluster
Discussion of Colfax Cluster usage policies, troubleshooting.

Developer Training, HOW Series
Questions about any of the Colfax trainings? Usage of training servers, experience with specific exercises, inquiries on what's inside, suggestions for future trainings - post them here.

Performance Optimization and Parallelism
Discuss with Colfax Research and colleagues any topics related to computational science, parallel programming, performance optimization and code modernization.

colfaxresearch.com/discussion

- ▶ All registrants receive an invitation from `cluster@colfaxresearch.com`
- ▶ Queue-based access to Intel Xeon E5, Intel Xeon Phi (KNC and KNL)
- ▶ Can access the cluster the entire 2 weeks of the workshop





§2. REFRESH



PERFORMANCE OPTIMIZATION

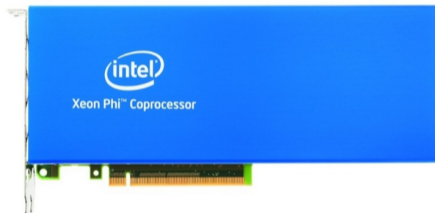
Intel Xeon Processor



Current: Broadwell
Upcoming: Skylake

Multi-Core Architecture

Intel Xeon Phi Coprocessor, 1st generation



Knights Corner (KNC)

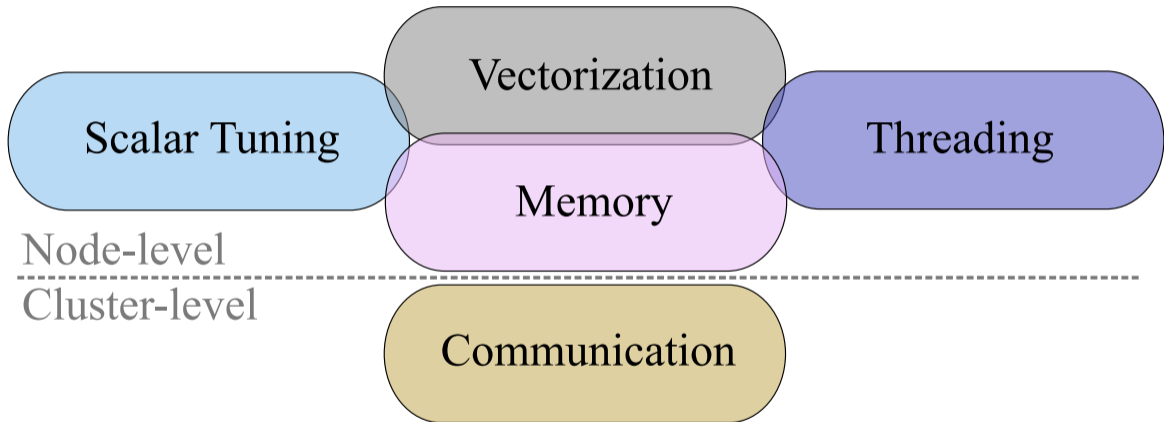
Intel Xeon Phi Processor, 2nd generation*



* socket and coprocessor versions

Knights Landing (KNL)

Intel Many Integrated Core (MIC) Architecture





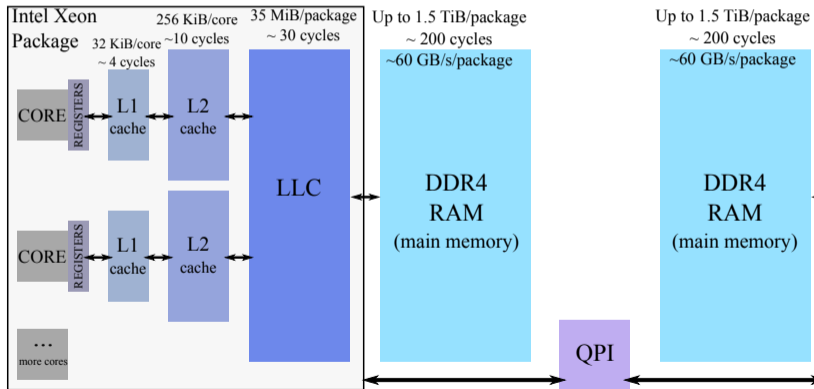
§3. MEMORY TRAFFIC TUNING



MEMORY HIERARCHY

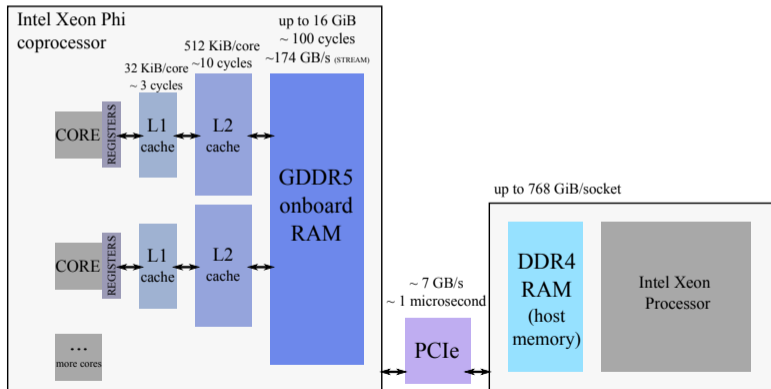
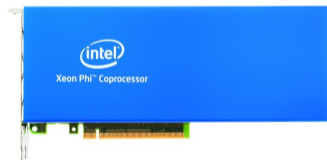
INTEL XEON CPU: MEMORY ORGANIZATION

- ▶ Hierarchical cache structure
- ▶ Two-way processors have NUMA architecture



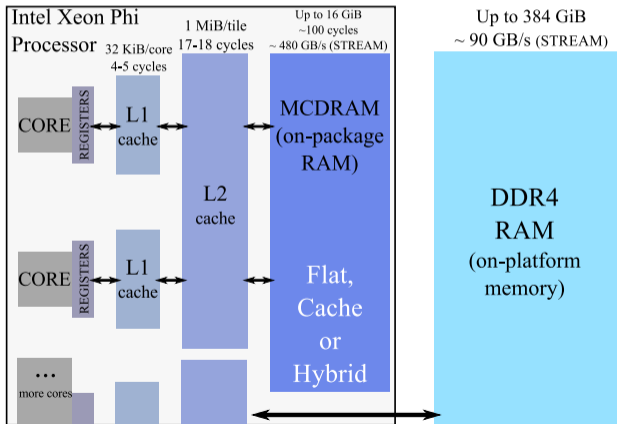
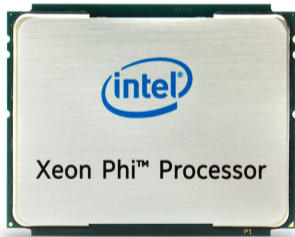
KNC MEMORY ORGANIZATION

- ▶ Direct access to ≤ 16 GiB of cached GDDR5 memory on board
- ▶ No access to system DDR4, connected to host via PCIe

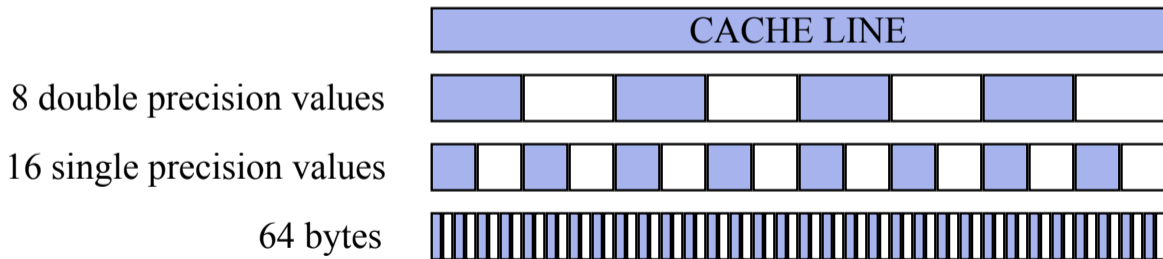


KNL MEMORY ORGANIZATION (BOOTABLE)

- ▶ On-package high-bandwidth memory (HBM) – MCDRAM
- ▶ Optimized for arithmetic performance and bandwidth (not latency)



- ▶ Minimal block of data transferred between memory and cache
- ▶ 64 bytes long in Intel Architecture
- ▶ Aligned on 64-byte boundaries in memory



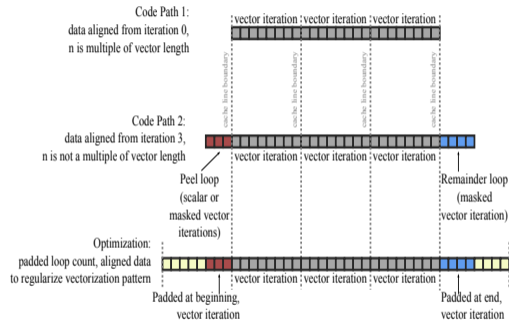


MEMORY RE-USE AND ALGORITHMS

LOOP WAS VECTORIZED, NOW WHAT?

1. Unit-stride access
2. Data alignment
3. Container padding
4. Eliminate peel loops
5. Eliminate multiversioning
6. **Optimize data re-use in caches**

```
for (i = 0; i < n; i++) A[i] = ...
```



LOOP WAS VECTORIZED, NOW WHAT?

1. Unit-stride access
2. Data alignment
3. Container padding
4. Eliminate peel loops
5. Eliminate multiversioning
6. **Optimize data re-use in caches**

Vector Arithmetics is Cheap, Memory Access is Expensive

If you don't optimize cache usage, vectorization will not matter.

You will be bottlenecked by memory access.



Intel Xeon Phi processor 7250

$68 \text{ cores} \times 1.2 \text{ GHz} \times 8 \text{ vec.lanes} \times 2 \text{ FMA} \times 2 \text{ IPC} \approx 2.6 \text{ TFLOP/s}$

$2.6 \text{ TFLOP/s} \times 8 \text{ bytes} \approx 21 \text{ TB/s}$

MCDRAM bandwidth $\approx 0.48 \text{ TB/s}$

Ratio = $21/0.48 \approx 43 \text{ (FLOPs)/(Memory Access)}$

- ▶ $> 50 \text{ FLOPs/Memory Access}$ — Compute-bound Application
- ▶ $< 50 \text{ FLOPs/Memory Access}$ — Bandwidth-bound Application

MEMORY ACCESS VERSUS ARITHMETICS IN KNL

Most values in cycles. Lower is better.

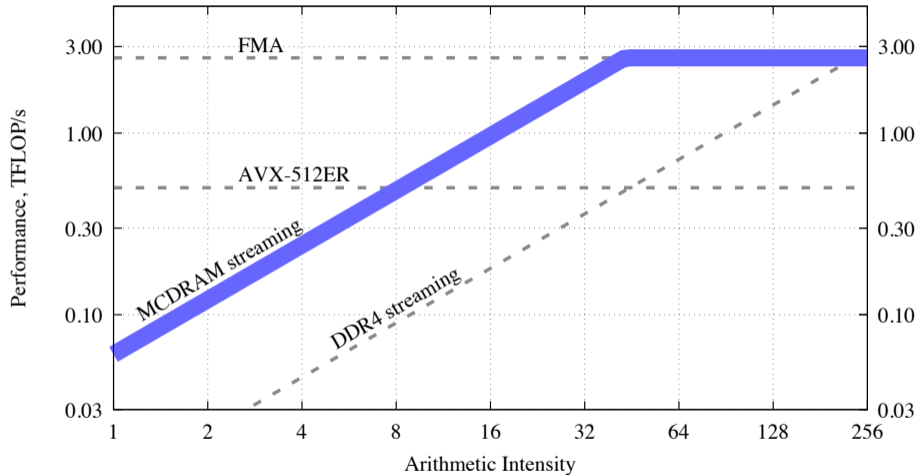
Instruction	Latency	1/Throughput
Most vector math and FMA	6	0.5
exp2a23, rcp28 and rsqrt28	7-8	2-3
Floating-point division and sqrt	38	10
Contiguous load	5	0.5
Gather 8 (16) elements	15 (19)	5 (10)
L1 cache access	4-5	0.5 → >12 TB/s
L2 cache access	13+L1 latency	
MCDRAM access	150-160 ns	>450 GB/s
DDR4 access	125-140 ns	>90 GB/s

ON COMPUTATIONAL COMPLEXITY OF ALGORITHMS

Type	Properties	Examples
$O(N)$	Each data element is used a fixed number of times. Memory-bound unless the number of times is large.	Array scaling, image brightness adjustment, vector dot-product.
$O(N^\alpha)$	Each element is used $N^{\alpha-1}$ times. A lot of data reuse for $\alpha > 1$. Good implementation can be compute-bound, poor one – memory-bound.	Matrix-matrix multiplication: $O(N^{3/2})$ (N = amount of data in matrix), direct N-body calculation: $O(N^2)$
$O(N \log N)$	Each element is used $\log N$ times. For small problems – memory-bound, for very large problems transitions to compute-bound	Fast Fourier transform, merge sort
$O(\log N)$	Always memory-bound.	Binary search

N = data size

ARITHMETIC INTENSITY AND ROOFLINE MODEL



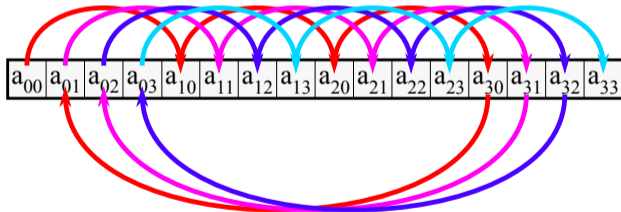
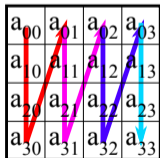
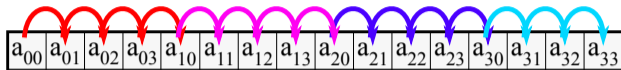
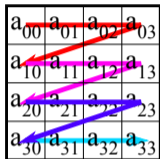
More on roofline model: [Williams et al.](#)



LOOP PERMUTATION

PRINCIPLE

Choose loop order to maintain unit-stride memory access



Compiler may or may not be able to automate loop permutation.

EXAMPLE: OVER-SIMPLIFIED MATRIX-MATRIX MULTIPLICATION

$$C = AB \quad \Leftrightarrow \quad C_{ij} = \sum_{k=0}^{n-1} A_{ik} B_{kj}$$

Before:

```

1  #pragma omp parallel for
2  for (int i = 0; i < n; i++)
3      for (int j = 0; j < n; j++)
4      #pragma vector aligned
5          for (int k = 0; k < n; k++)
6              C[i*n+j] += A[i*n+k] * B[k*n+j];

```

After:

```

1  #pragma omp parallel for
2  for (int i = 0; i < n; i++)
3      for (int k = 0; k < n; k++)
4      #pragma vector aligned
5          for (int j = 0; j < n; j++)
6              C[i*n+j] += A[i*n+k] * B[k*n+j];

```

PRINCIPLE

- ▶ For best spatial locality, order loops to get unit-stride
- ▶ At `-O2` and above, the compiler may interchange loops
- ▶ In complex cases, investigate loop interchange manually
- ▶ May need to re-design data containers to get unit stride

LOOP FUSION

LOOP FUSION TECHNIQUE

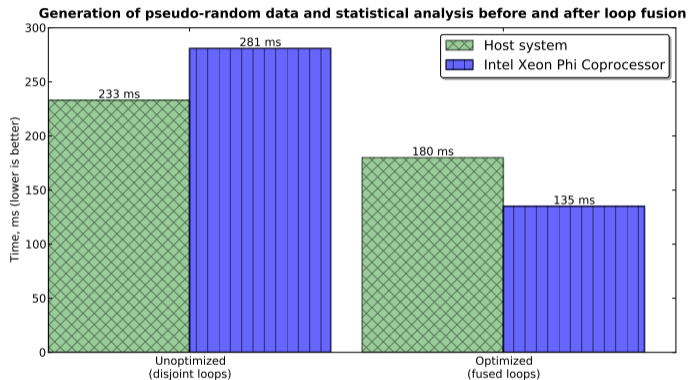
Re-use data in cache by fusing loops in a data processing pipeline

```
1 MyData* data = new MyData(n);
2
3 for (int i = 0; i < n; i++)
4     Initialize(data[i]);
5
6 for (int i = 0; i < n; i++)
7     Stage1(data[i]);
8
9 for (int i = 0; i < n; i++)
10    Stage2(data[i]);
```

```
1 MyData* data = new MyData(n);
2
3 for (int i = 0; i < n; i++) {
4
5     Initialize(data[i]);
6
7     Stage1(data[i]);
8
9     Stage2(data[i]);
10 }
```

Potential positive side-effect: less data to carry between stages, reduced memory footprint, improved performance.

EXAMPLE APPLICATION -- PERFORMANCE



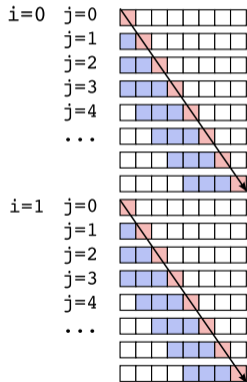
See [labs/4/4.09-memory-loop-fusion-statistics/](#)

LOOP TILING

LOOP TILING: CACHE BLOCKING

Original:

```
for (i=0; i<m; i++)
  for (j=0; j<n; j++)
    ...=...*b[j];
```



- - cached, LRU eviction policy
- - cache miss (read from memory, slow)
- - cache hit (read from cache, fast)

Cache size: 4

TILE=4

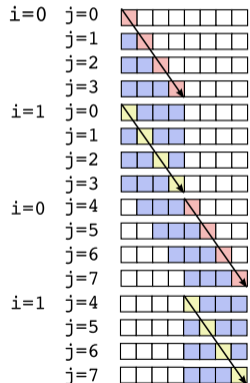
(must be tuned to cache size)

Cache hit rate without tiling: 0%

Cache hit rate with tiling: 50%

Tiled:

```
for (jj=0; jj<n; jj+=TILE)
  for (i=0; i<m; i++)
    for (j=jj; j<jj+TILE; j++)
      ...=...*b[j];
```



LOOP TILING (CACHE BLOCKING) -- PROCEDURE

```

1  for (int i = 0; i < m; i++) // Original code:
2      for (int j = 0; j < n; j++)
3          compute(a[i], b[j]); // Memory access is unit-stride in j

```

```

1  // Step 1: strip-mine inner loop
2  for (int i = 0; i < m; i++)
3      for (int jj = 0; jj < n; jj += TILE)
4          for (int j = jj; j < jj + TILE; j++)
5              compute(a[i], b[j]); // Same order of operation as original

```

```

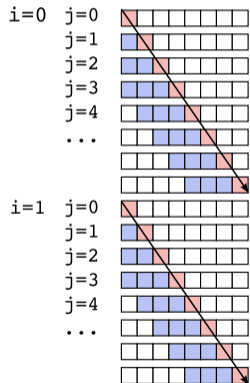
1  // Step 2: permute
2  for (int jj = 0; jj < n; jj += TILE)
3      for (int i = 0; i < m; i++)
4          for (int j = jj; j < jj + TILE; j++)
5              compute(a[i], b[j]); // Re-use to j=jj sooner

```

LOOP TILING: REGISTER BLOCKING

Original:

```
for (i=0; i<m; i++)
  for (j=0; j<n; j++)
    ...=*b[j];
```



- - cached, LRU eviction policy
- - cache miss (read from memory, slow)
- - cache hit (read from cache, fast)

Cache size: 4

TILE=4

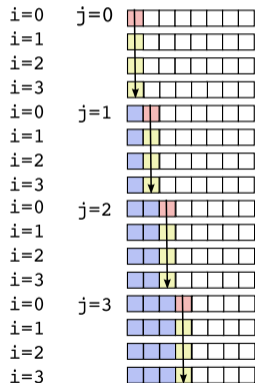
(must be tuned to cache size)

Cache hit rate without tiling: 0%

Cache hit rate with tiling: 50%

Tiled:

```
for (ii=0; ii<m; ii+=TILE)
  for (j=0; j<n; j++)
    for (i=ii; i<ii+TILE; i++)
      ...=*b[j];
```



LOOP TILING (UNROLL-AND-JAM/REGISTER BLOCKING)

```

1  for (int i = 0; i < m; i++) // Original code:
2      for (int j = 0; j < n; j++)
3          compute(a[i], b[j]); // Memory access is unit-stride in j

```

```

1  // Step 1: strip-mine outer loop
2  for (int ii = 0; ii < m; ii += TILE)
3      for (int i = ii; i < ii + TILE; i++)
4          for (int j = 0; j < n; j++)
5              compute(a[i], b[j]); // Same order of operation as original

```

```

1  // Step 2: permute and vectorize outer loop
2  for (int ii = 0; ii < m; ii += TILE)
3  #pragma simd
4      for (int j = 0; j < n; j++)
5          for (int i = ii; i < ii + TILE; i++)
6              compute(a[i], b[j]); // Use each vector in b[j] a total of TILE times

```

LOOP TILING (UNROLL-AND-JAM) -- ALTERNATIVE IMPLEMENTATION

```

1  for (int i = 0; i < m; i++)    // Original code:
2      for (int j = 0; j < n; j++)
3          compute(a[i], b[j]); // Memory access is unit-stride in j

```

```

1  // Step 1: strip-mine both loops
2  for (int ii = 0; ii < m; ii += TILE)
3      for (int i = ii; i < ii + TILE; i++)
4          for (int jj = 0; jj < n; jj += VECLLEN)
5              for (int j = jj; j < jj + VECLLEN; j++)
6                  compute(a[i], b[j]); // Same order of operation as original

```

```

1  // Step 2: permute middle two loops
2  for (int ii = 0; ii < m; ii += TILE)
3      for (int jj = 0; jj < n; jj += VECLLEN)
4          for (int i = ii; i < ii + TILE; i++)
5              for (int j = jj; j < jj + VECLLEN; j++)
6                  compute(a[i], b[j]); // Use each vector in b[j] a total of TILE times

```



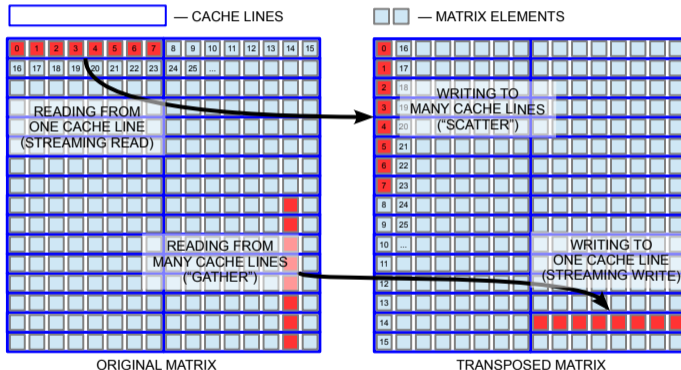
CACHE-OBLIVIOUS RECURSION



EXAMPLE 1: MATRIX TRANSPOSITION, TILING

LOOP TILING EXAMPLE: MATRIX TRANSPOSITION

$$B = A^T \quad \Leftrightarrow \quad B_{ij} = A_{ji}$$



See also [this paper](#).

MATRIX TRANSPOSITION

Before:

```
1  #pragma omp parallel for
2  for (int i = 0; i < n; i++)
3      for (int j = 0; j < n; j++)
4          B[i*n + j] = A[j*n + i];
```

After:

```
1  const int tile = 200;
2  if (n%tile != 0) exit(1);
3
4  #pragma omp parallel for
5  for (int ii=0; ii<n; ii+=tile)
6      for (int jj=0; jj<n; jj+=tile)
7          for (int i=ii; i<ii+tile; i++)
8              for (int j=jj; j<jj+tile; j++)
9                  B[i*n + j] = A[j*n + i];
```



EXAMPLE 2: MATRIX-VECTOR MULTIPLICATION, TILING

EXAMPLE: MATRIX-VECTOR MULTIPLICATION

$$c_i = \sum_{j=0}^n A_{ij} b_j, \quad i = 0, 1, \dots, (m-1). \quad (1)$$

```

1 void Multiply(const double* const A, const double* const b,
2              double* const c, const long n, const long m){
3     assert(n%64 == 0);
4     #pragma omp parallel for
5     for (long i = 0; i < m; i++)
6     #pragma vector aligned
7         for (long j = 0; j < n; j++) // Each value of A[i*n+j] is used only once
8             c[i] += A[i*n+j] * b[j]; // Each value of b[j] is used a total of m times
9 }

```

Non-optimal performance due to inefficient cache use

APPLYING TILING

```

1  const long jTile = 4096L; assert(n%jTile == 0);
2  #pragma omp parallel
3  {
4      double temp_c[m] __attribute__((aligned(64)));
5      temp_c[:] =0;
6      #pragma omp for
7          for (long jj =0; jj < n; jj+=jTile) // Loop Tiling in j
8              for (long i = 0; i < m; i++)
9                  #pragma vector aligned
10                     for (long j =jj; j < jj+jTile; j++)
11                         temp_c[i] += A[i*n+j] * b[j];
12
13     for(long i = 0; i < m; i++) { // Reduction
14         #pragma omp atomic
15             c[i]+= temp_c[i];
16     } } }

```

CACHE BLOCKING + STRIP-MINE AND COLLAPSE

```
1  const long iTile = 64L;    assert(m%iTile == 0);
2  const long jTile = 4096L; assert(n%jTile == 0);
3  #pragma omp parallel
4  {
5      double temp_c[m] __attribute__((aligned(64))); temp_c[:] =0;
6  #pragma omp for collapse(2)
7      for (long ii = 0; ii < m; ii += iTile)
8          for (long jj = 0; jj < n; jj += jTile)
9              for (long i = ii; i < ii+iTile; i++)
10 #pragma vector aligned
11                 for (long j =jj; j < jj+jTile; j++)
12                     temp_c[i] += A[i*n+j] * b[j];
13
14     for(long i = 0; i < m; i++) {
15 #pragma omp atomic
16         c[i]+= temp_c[i];
17 } } }
```



EXAMPLE 3: MATRIX-VECTOR MULTIPLICATION, RECURSION

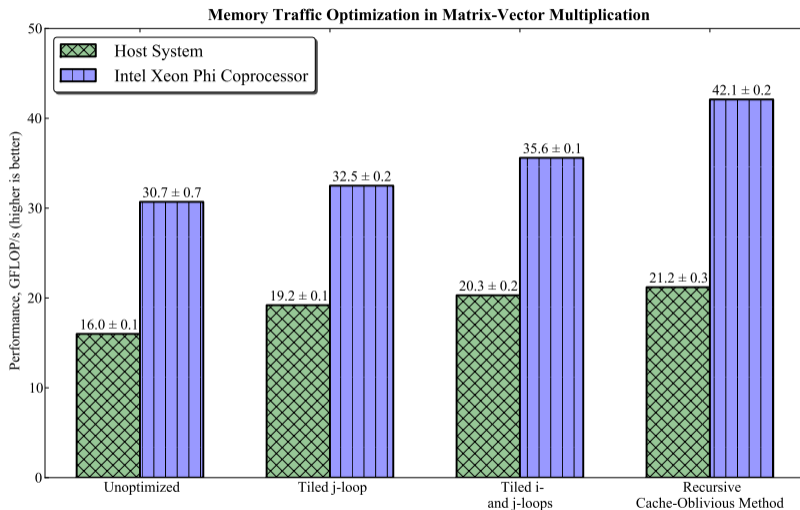
EXAMPLE: MATRIX-VECTOR MULTIPLICATION

```

1 void RecursMultiply(const double* const A, const double* const b,
2     double* const c, const long n, const long m, const long lda){
3     const long jThreshold = 8192L; assert(n%jThreshold == 0);
4     const long iThreshold = 64L;  assert(m%iThreshold == 0);
5     if ((m<=iThreshold) && (n<=jThreshold)) { // Recursion threshold
6         // .... Base Case: Compute the result inside the tile ... //
7     } else { // Recursive divide-and-conquer
8         if (m*jThreshold > n*iThreshold) { // Split i-wise
9             double c1[m/2] __attribute__((aligned(64)));
10 #pragma omp task
11     { RecursMultiply(&A[0*lda + 0], &b[0], c1, n, m/2, lda); }
12     double c2[m/2] __attribute__((aligned(64)));
13     RecursMultiply(&A[(m/2)*lda + 0], &b[m/2], c2, n, m/2, lda);
14 #pragma omp taskwait
15     c[0:m/2] += c1[0:m/2]; c[m/2:m/2] += c2[0:m/2]; // Reduction
16     } else { // .... Split j-wise .... // }
17 } }

```

PERFORMANCE OF MATRIX VECTOR MULTIPLICATION

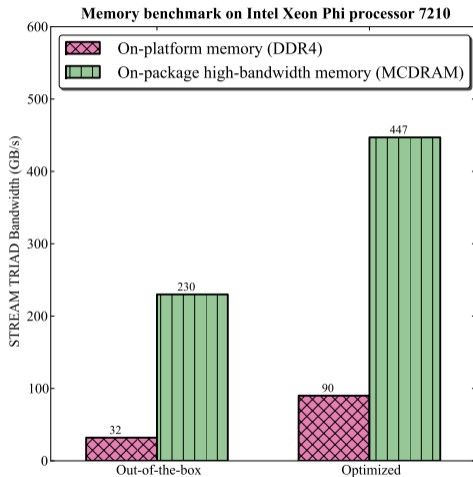




BANDWIDTH TUNING

STREAM BENCHMARK

- ▶ Industry-standard tool for memory bandwidth measurement
- ▶ 4 tests: COPY, ADD, SCALE and TRIAD
- ▶ Download from Dr. John McCalpin's site:
www.cs.virginia.edu/stream/



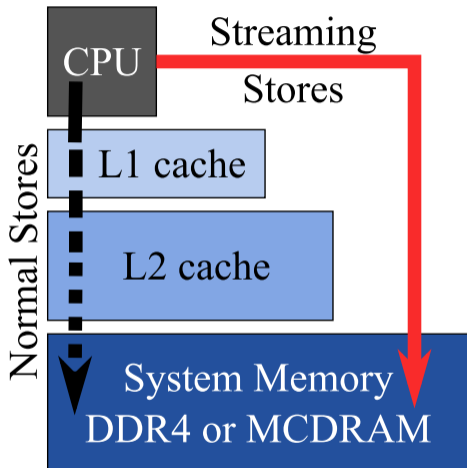
STREAM BENCHMARK TUNING

- ▶ KNL: Compile with `-xMIC-AVX512` (see also [HOW Series “KNL”](#))
- ▶ Set large enough array size: `-DSTREAM_ARRAY_SIZE=64000000`
- ▶ Set 1 thread per core (`-1` for offload)
- ▶ Xeon CPU: set affinity “[scatter](#)” (default on Xeon Phi)
- ▶ KNC: Tune prefetching ([learn more](#))

In addition, secret sauce for your own STREAM-like application:

- ▶ Parallel first touch (see Session 8 of the [HOW Series](#))
- ▶ Essential element – streaming stores: [discussion](#)

STREAMING STORES

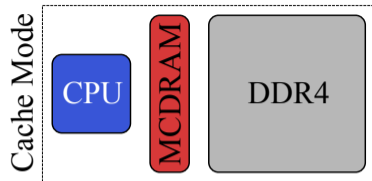


- ▷ Bypass cache, write to RAM
- ▷ Save cache for other data
- ▷ `#pragma vector nontemporal`
- ▷ `-qopt-streaming-stores=always`

USING HIGH-BANDWIDTH MEMORY (MCDRAM) IN KNL

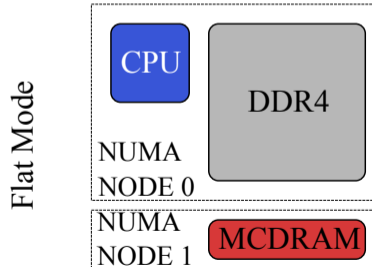
Option 1 : cache/hybrid mode

- ▶ Treat it as LLC
- ▶ Data locality techniques
- ▶ Miss latency 2x the direct DDR4 access



Option 2 : flat mode

- ▶ Application fits in 16 GiB? `numactl`
- ▶ More than 16 GiB data? Use special allocators (e.g., `memkind`)



BINDING TO NUMA NODES WITH `numactl`

- ▶ `libnuma` – a Linux library for fine-grained control over NUMA policy
- ▶ `numactl` – a tool for global NUMA policy control

```
vega@lyra% numactl --hardware
available: 2 nodes (0-1)
node 0 cpus: 0 1 2 3 4 5 12 13 14 15 16 17
node 0 size: 65457 MB
node 0 free: 24426 MB
node 1 cpus: 6 7 8 9 10 11 18 19 20 21 22 23
node 1 size: 65536 MB
node 1 free: 53725 MB
node distances:
node  0  1
  0:  10  21
  1:  21  10
vega@lyra% numactl --membind=<nodes> --cpunodebind=<nodes> ./myApplication
```

HBM IN KNIGHTS LANDING

- ▶ Finding HBM (MCDRAM) in an Intel Xeon Phi processor x200 (KNL):

```
user@knl% # In Flat mode with All-to-All or Quadrant
user@knl% numactl -H
available: 2 nodes (0-1)
node 0 cpus: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 ... 249 250 251 252 253 254 255
node 0 size: 98207 MB
node 0 free: 94798 MB
node 1 cpus:
node 1 size: 16384 MB
node 1 free: 15991 MB
```

- ▶ Binding the application to HBM (Flat/Hybrid)

```
user@knl% numactl --membind 1 ./runme
// ... Application running in HBM ... //
```



§4. REVIEW AND WHAT'S NEXT

Memory Optimization:

1. Data re-use in caches: increase arithmetic intensity
 - 1.1 Loop permutation: achieve unit-stride access
 - 1.2 Loop fusion: re-use data as soon as possible
 - 1.3 Loop tiling: cache blocking and unroll-and-jam
 - 1.4 Cache-oblivious recursion: portable
2. Access to main memory:
 - 2.1 1 thread/core, “scatter” affinity
 - 2.2 “Secret sauce” compiler arguments for KNC
 - 2.3 First-touch allocation in NUMA systems
 - 2.4 High-bandwidth memory (HBM) in KNL: numactl or memkind



§5. SUMMARY

WHAT WE LEARNED

- Session 1** Intel Architecture, Colfax Cluster
- Session 2** Programming Xeon Phi: native, offload, HBM, OPA
- Session 3** Expressing vectorization
- Session 4** Expressing thread parallelism (OpenMP)
- Session 5** Distributed computing (MPI)
- Session 6** Optimization overview (N-body)
- Session 7** Optimizing scalar component and vectorization
- Session 8** Optimizing multi-threading (common errors)
- Session 9** Optimizing multi-threading (memory aspect)
- Session 10** Optimizing memory access

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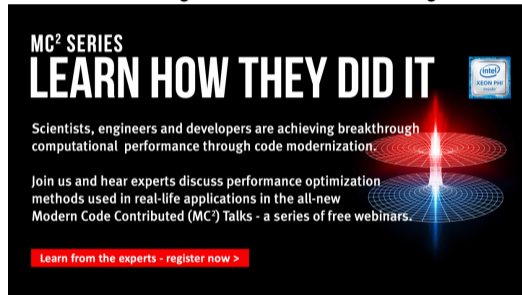
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The banner features a blue background with silhouettes of two divers underwater. A red box at the top contains the text 'THE "HOW" SERIES TRAINING'. The main title 'DEEP DIVE' is in large white letters, with 'WITH CODE MODERNIZATION EXPERTS' below it. A blue box with white text says 'It's free'. At the bottom, a line of text provides session details.

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